

Micro-mechanical investigation of yielding in cemented geo-materials

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CeIBA**

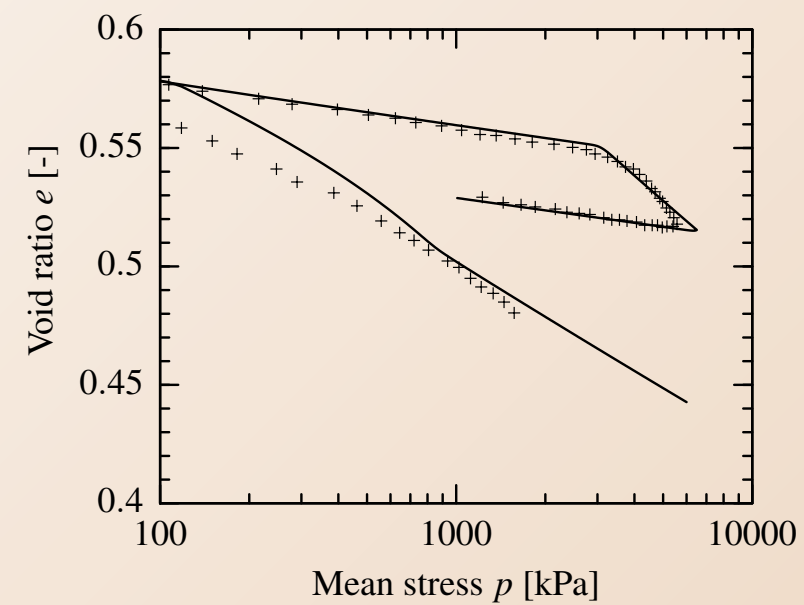
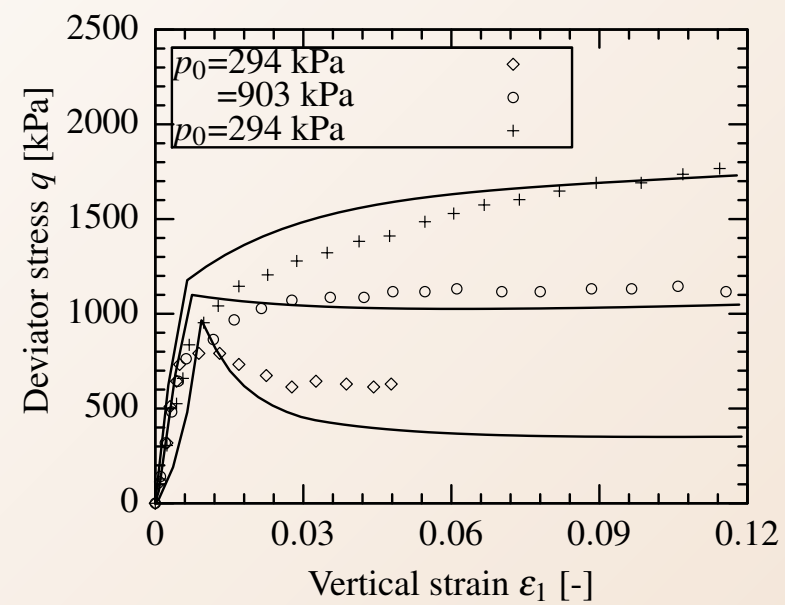
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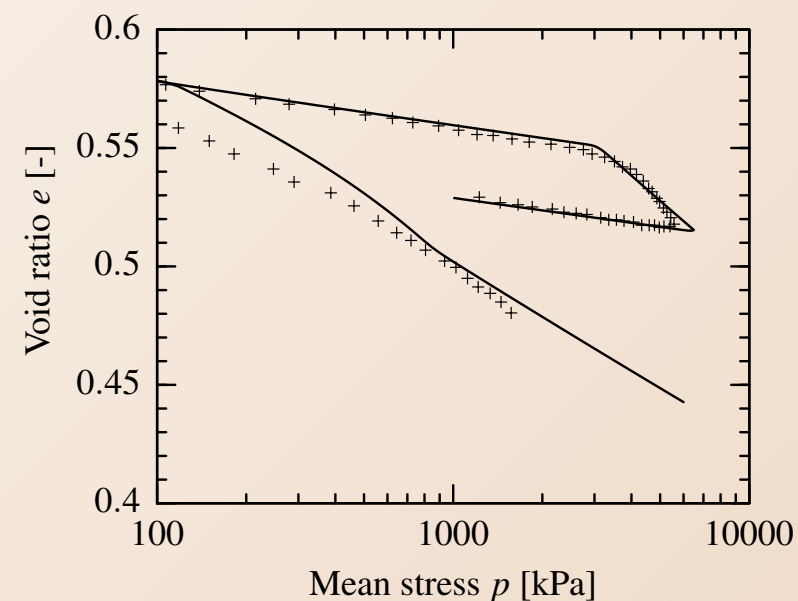
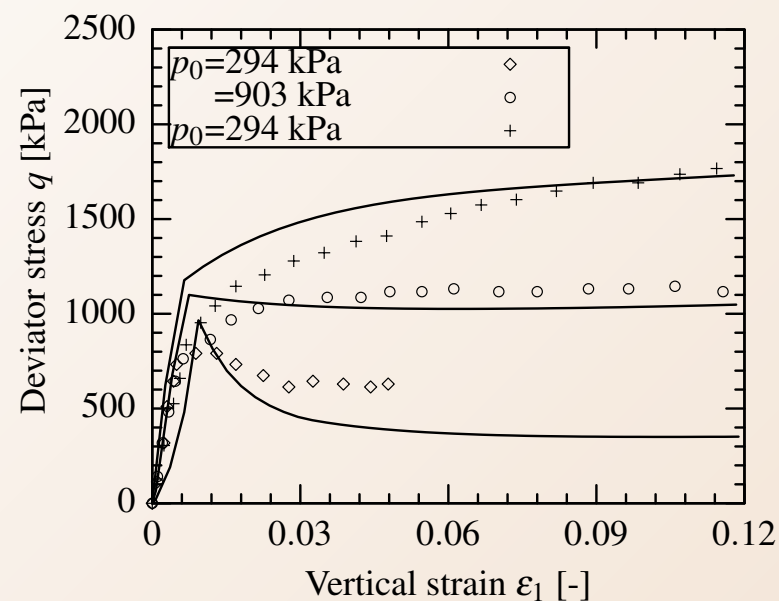


Motivation



Fuentes 2009, Simulation of a cemented granular soil using a modified Visco-hypoplastic constitutive model

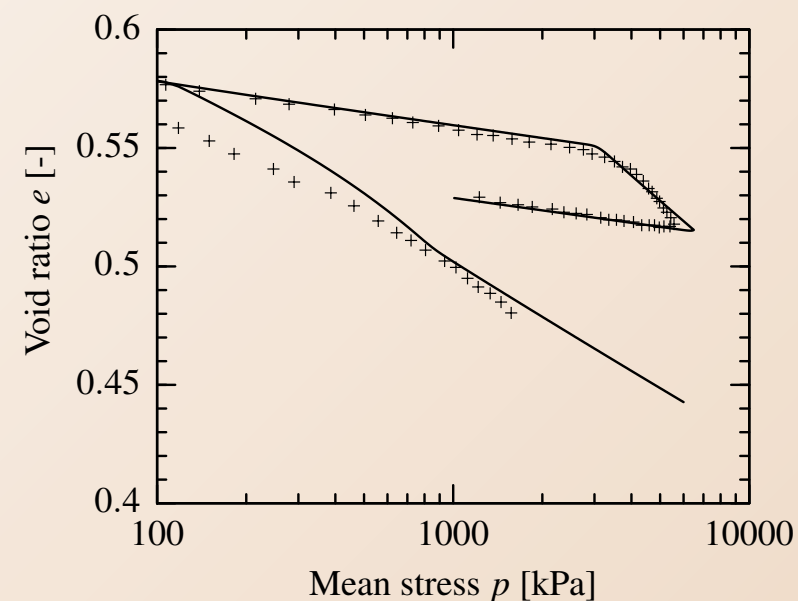
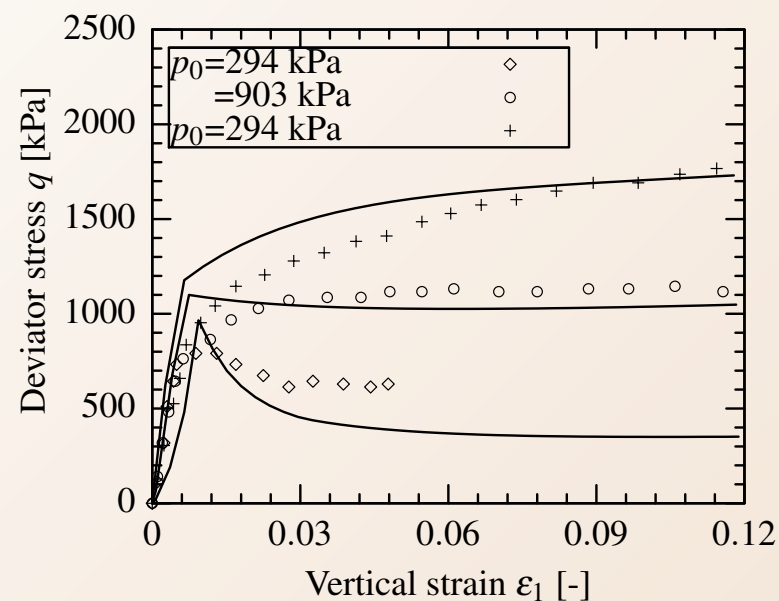
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Macroscopic models are **useful** to **describe** the behavior of granular cemented soils

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Fuentes 2009, Simulation of a cemented granular soil using a modified Visco-hypoplastic constitutive model

Macroscopic models are **useful** to **describe** the behavior of granular cemented soils

However, they represent a **limited tool** if we want to **explain** what is really happening at the grains scale

A privileged analysis tool:

➔ Discrete Element Methods

The purpose of this work is to investigate yielding
in cemented granular materials using
discrete element methods



Outline

1. Cementation model (Contact Dynamics)
3. Simple shear device
4. Macroscopic results
5. Microscopic analysis



I. Cementation model

Numerical method

Contact Dynamics (*J. J. Moreau & M. Jean*)

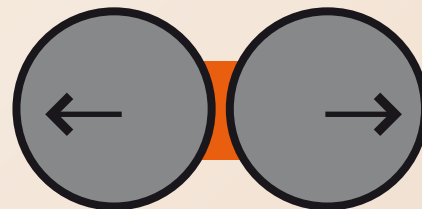
I. Cementation model

Numerical method

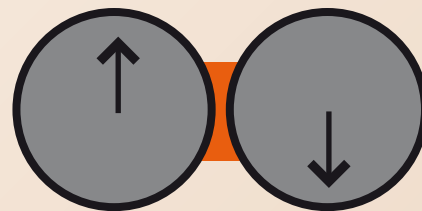
Contact Dynamics (*J.J. Moreau & M. Jean*)

Local cohesion model

Traction:

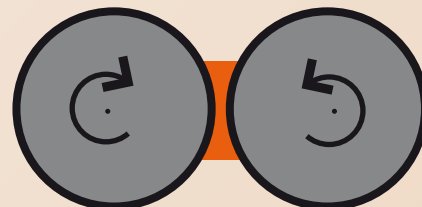


Shear:



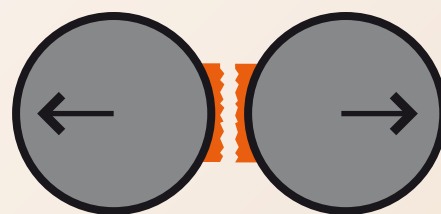
→ (*Coulomb's friction law*)

Flexion:

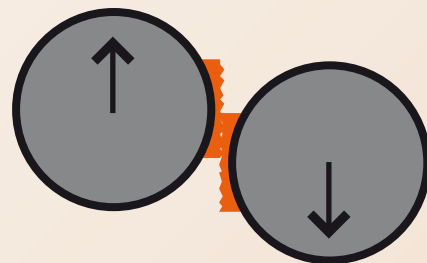


→ (*Contact law analogous to the Coulomb's friction law*)

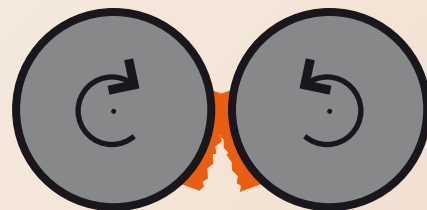
Local rupture conditions



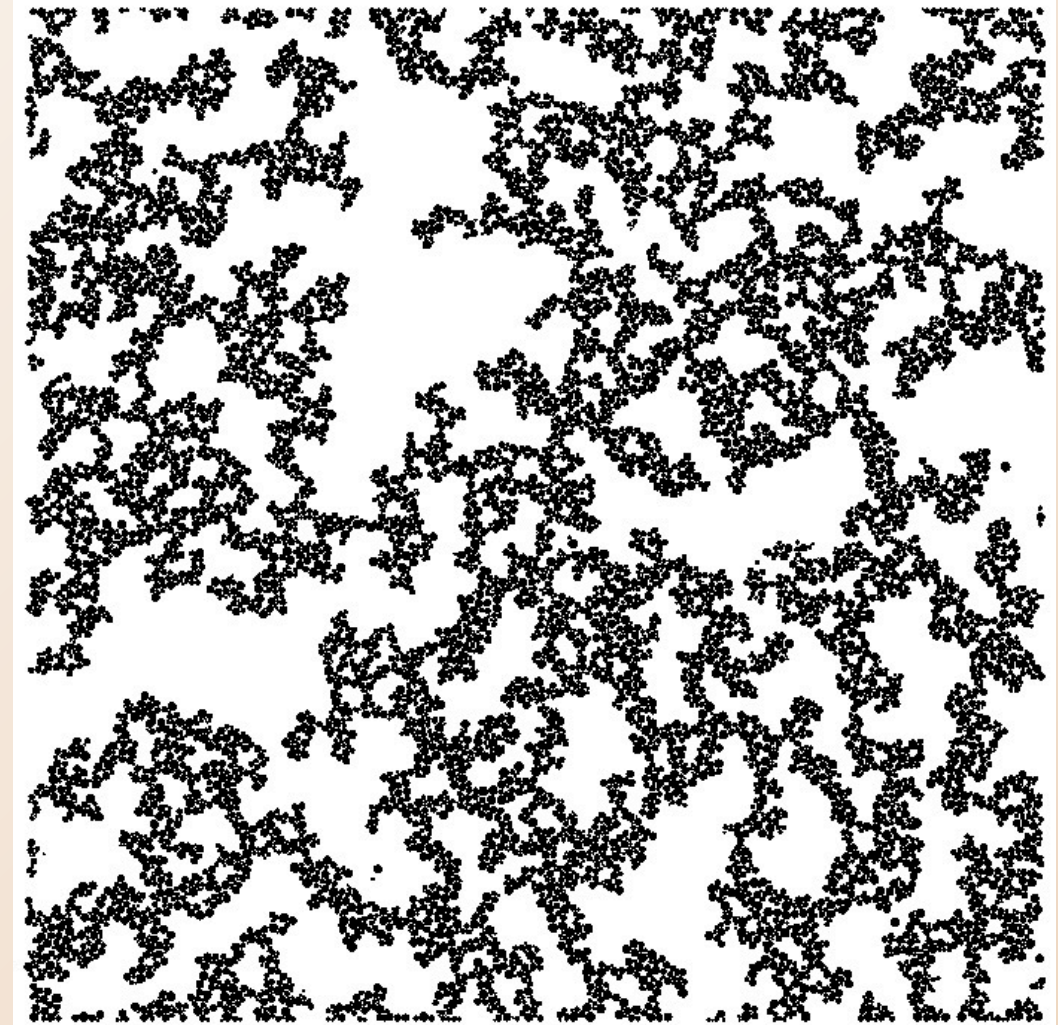
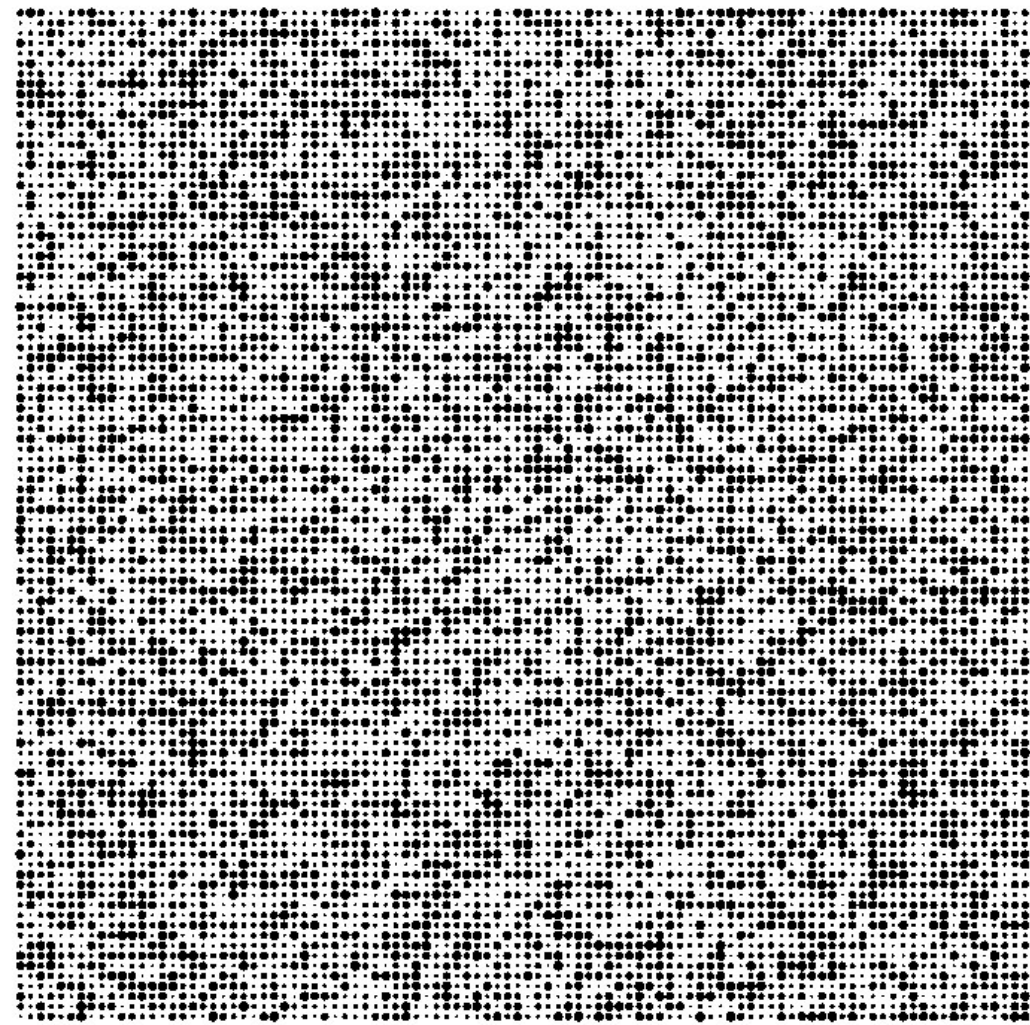
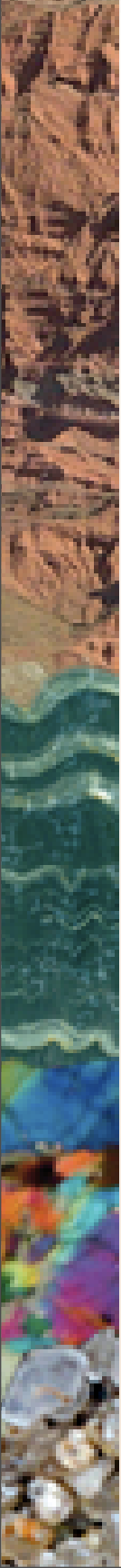
$$f_n = -f_a$$

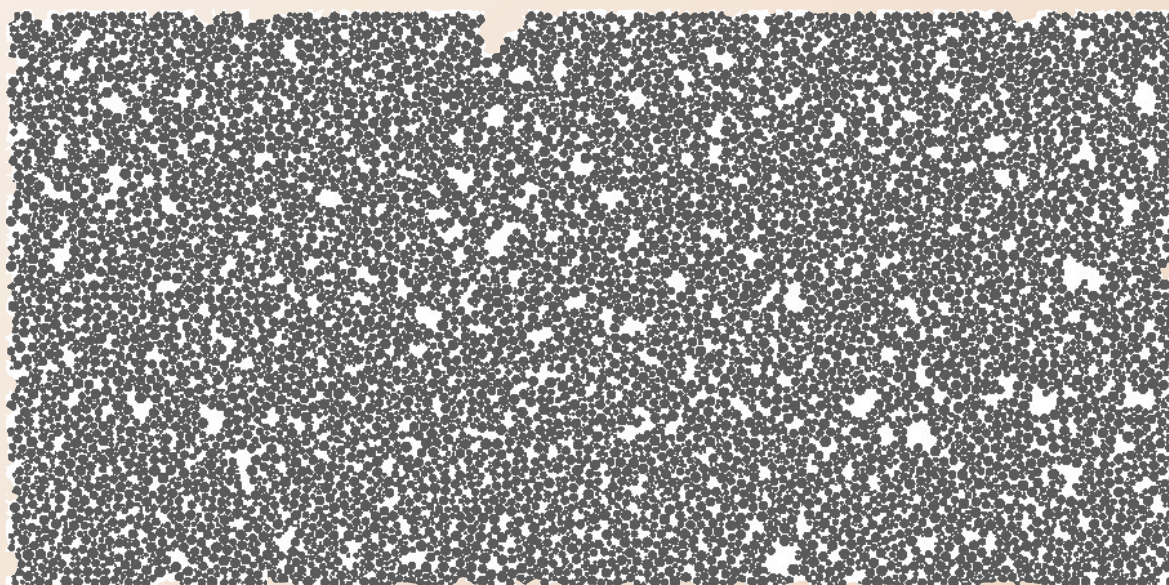
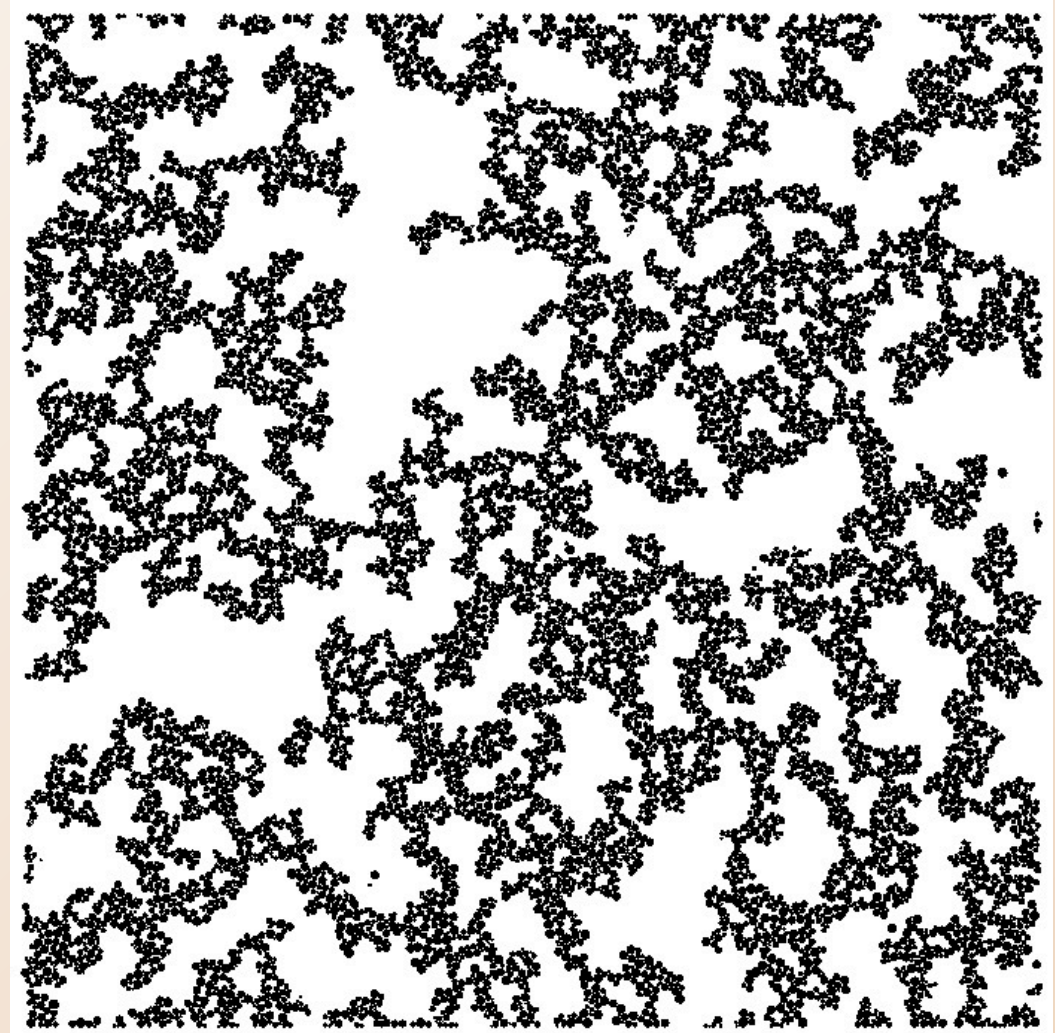
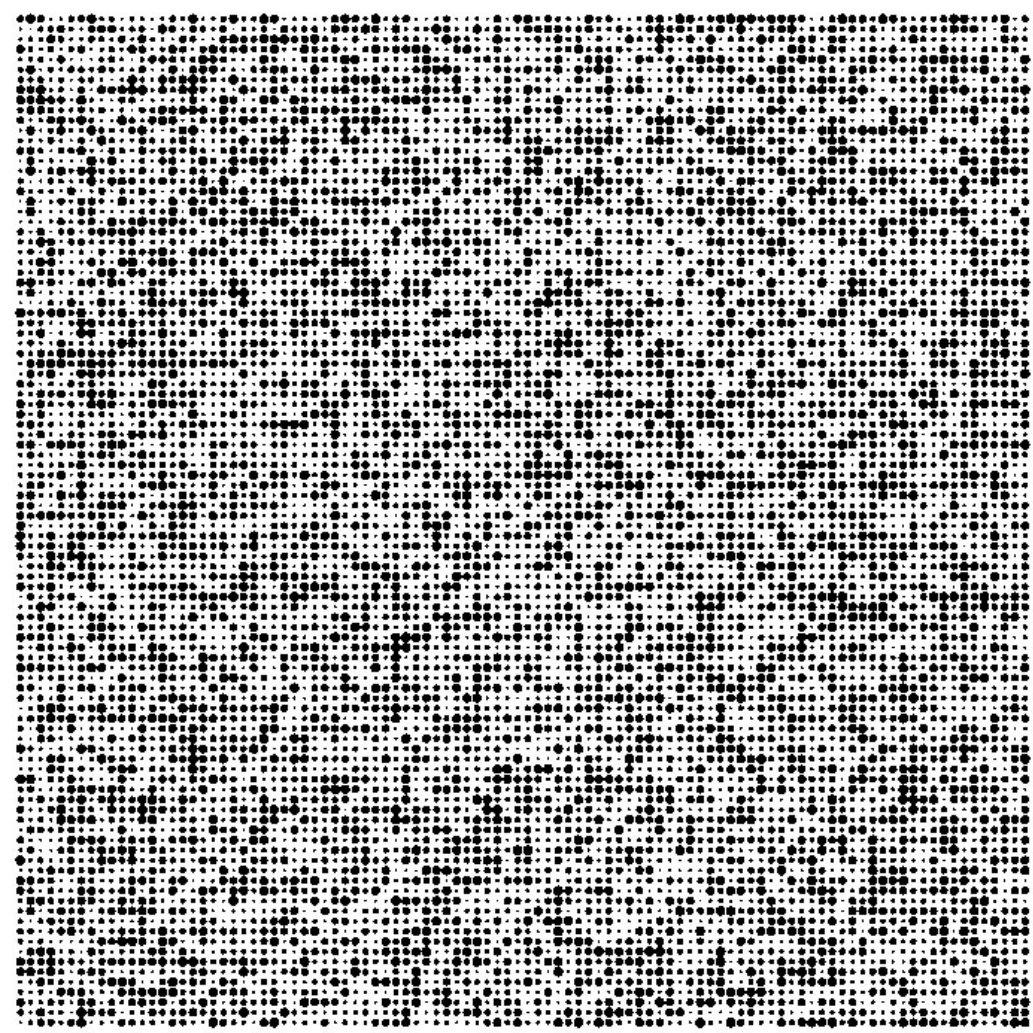


$$f_t = f_t^{max}$$

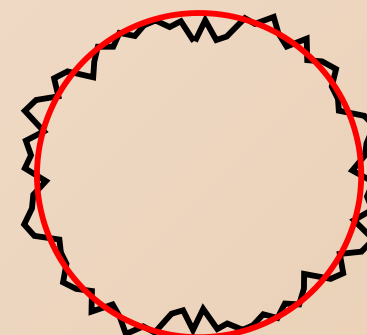
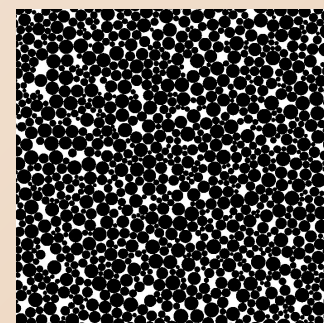
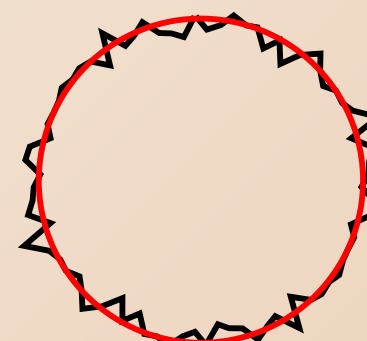
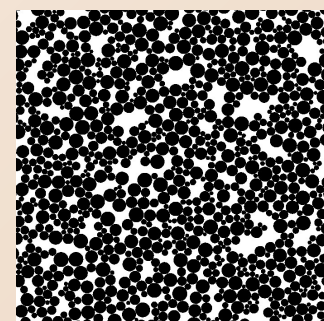
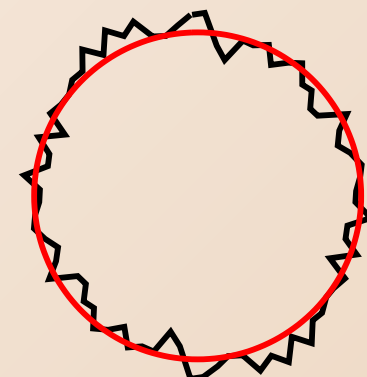
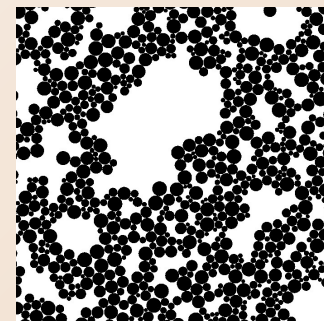
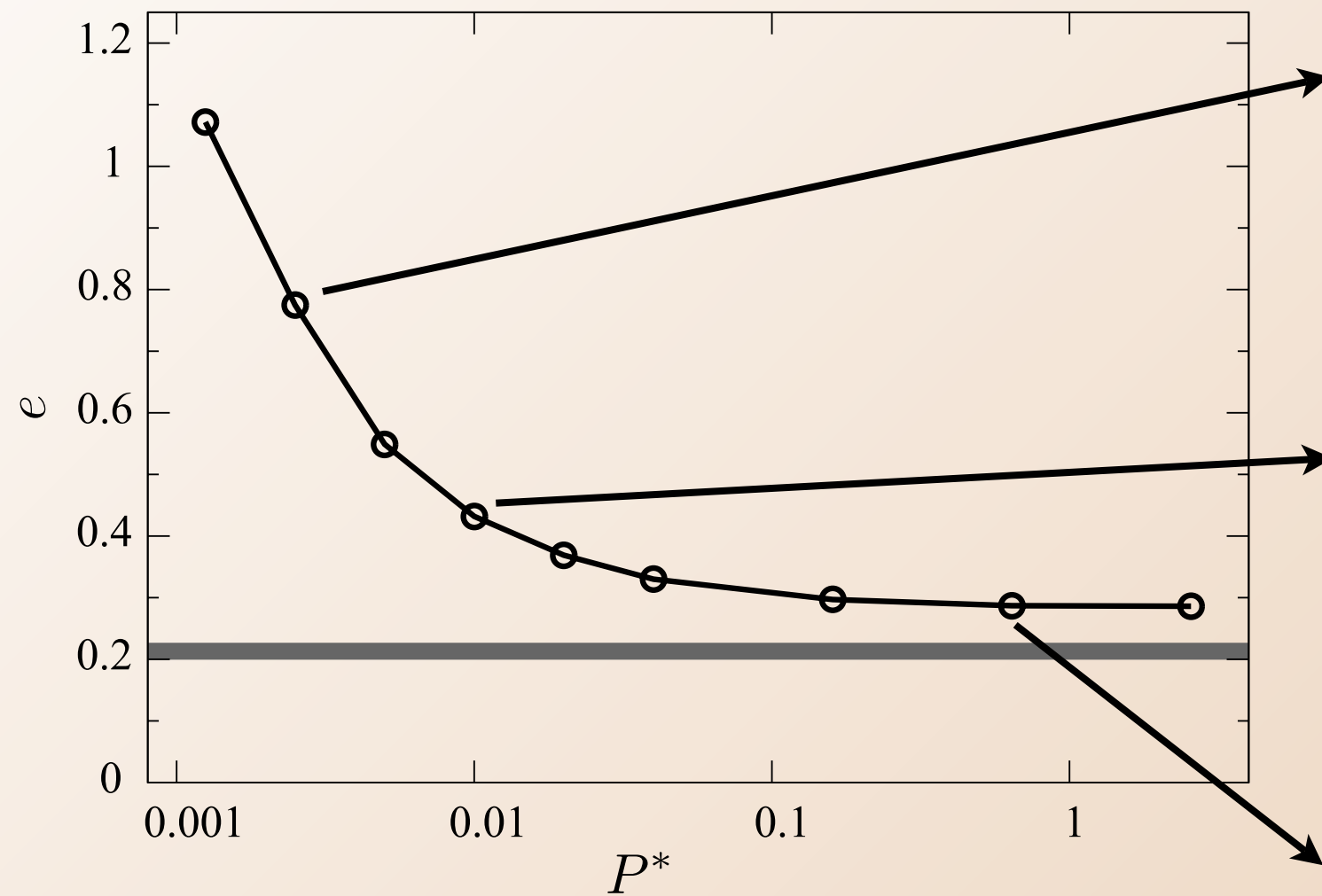


$$M = M^{max}$$



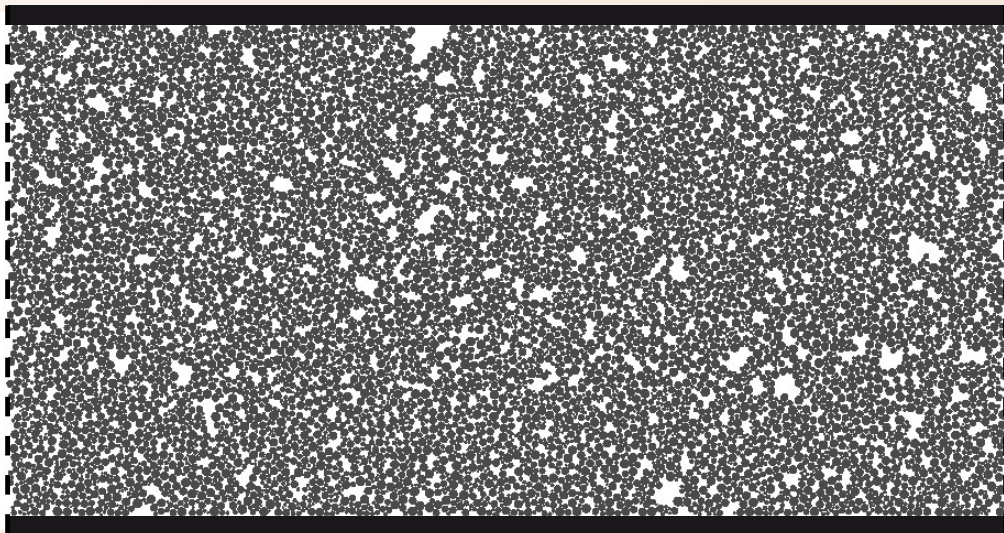


10.000 particles
 $e \simeq 0.42$

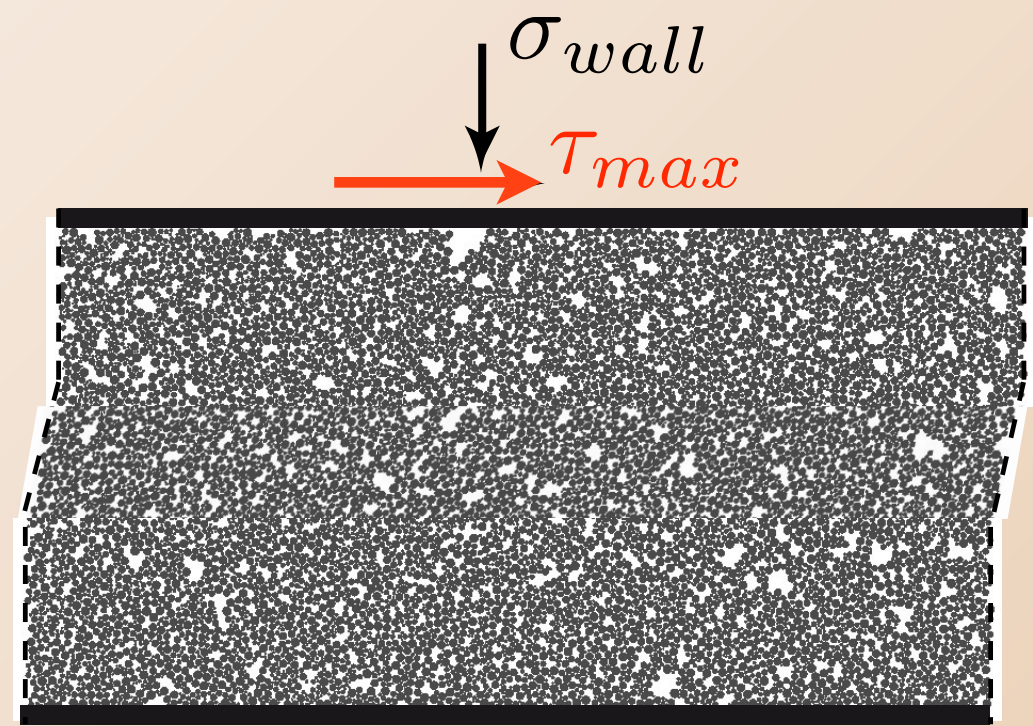
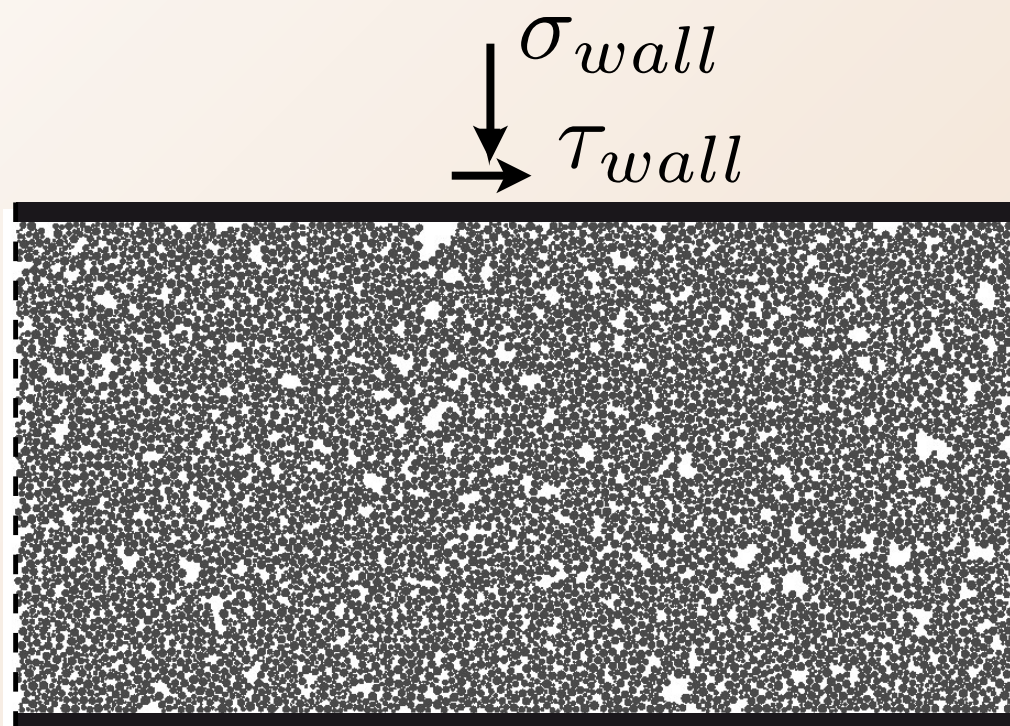


2. Simple shear device

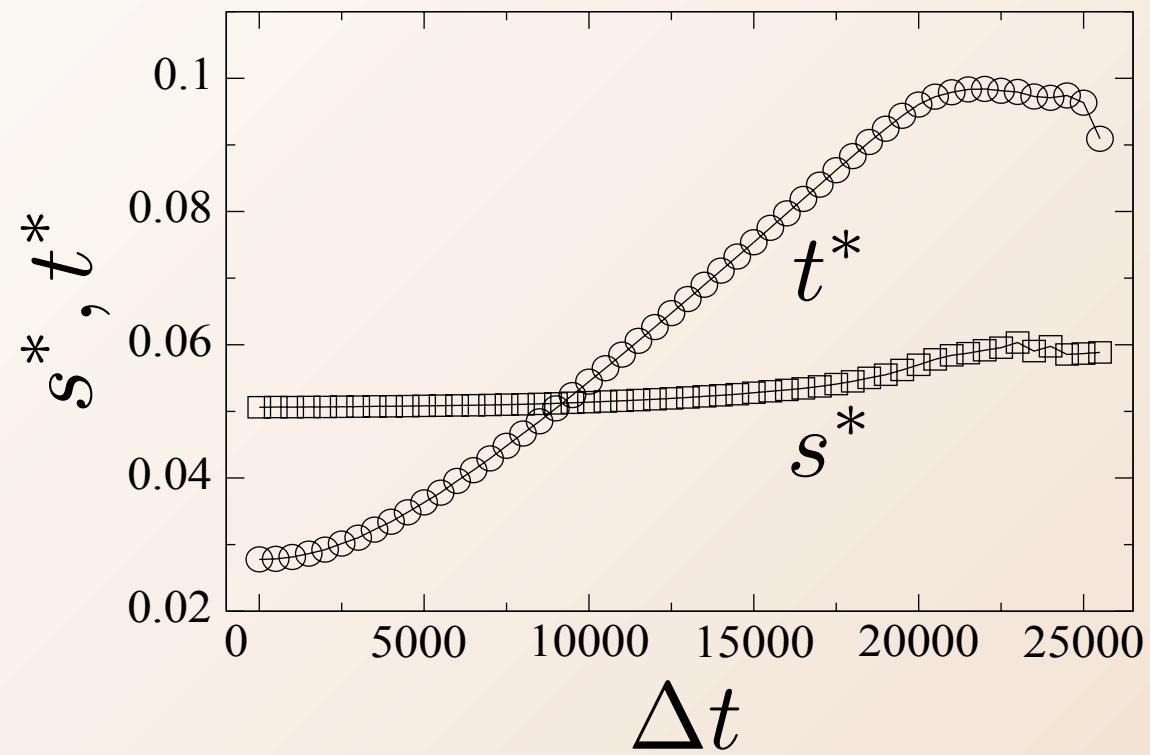
σ_{wall}
 τ_{wall}



2. Simple shear device



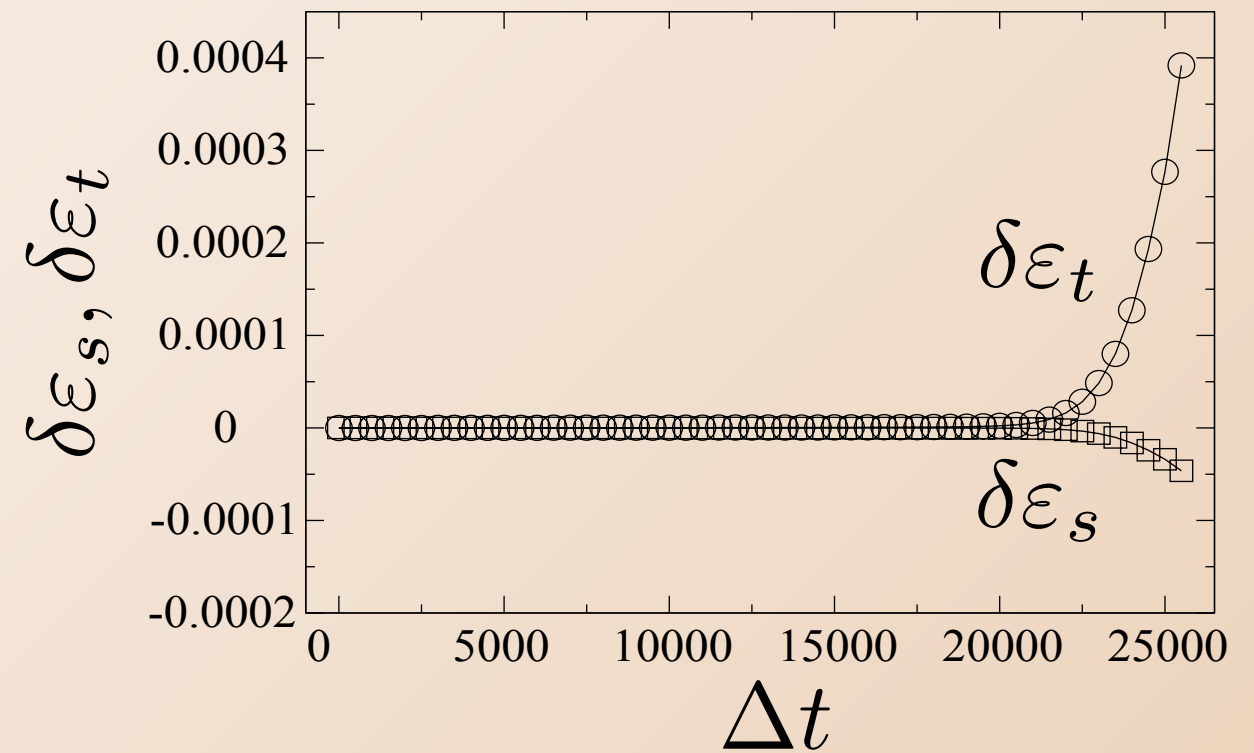
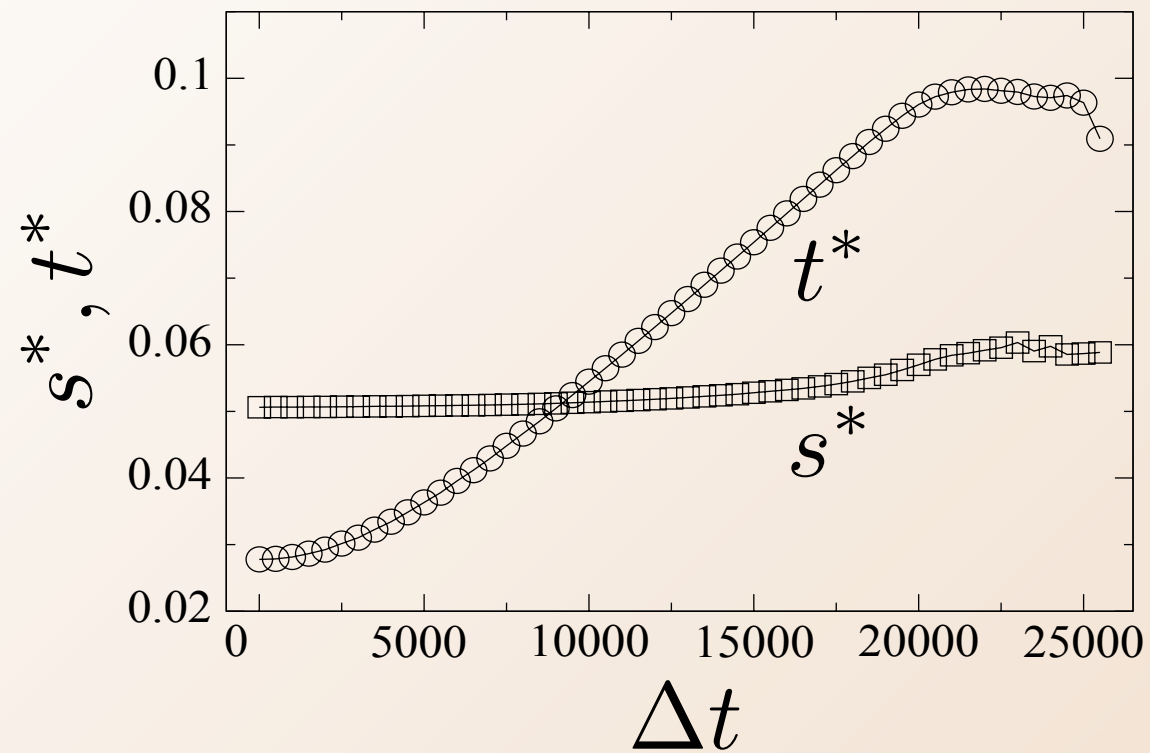
4. Macroscopic results



$$s^* \sim \frac{\sigma_1 + \sigma_3}{2}$$

$$t^* \sim \frac{\sigma_1 - \sigma_3}{2}$$

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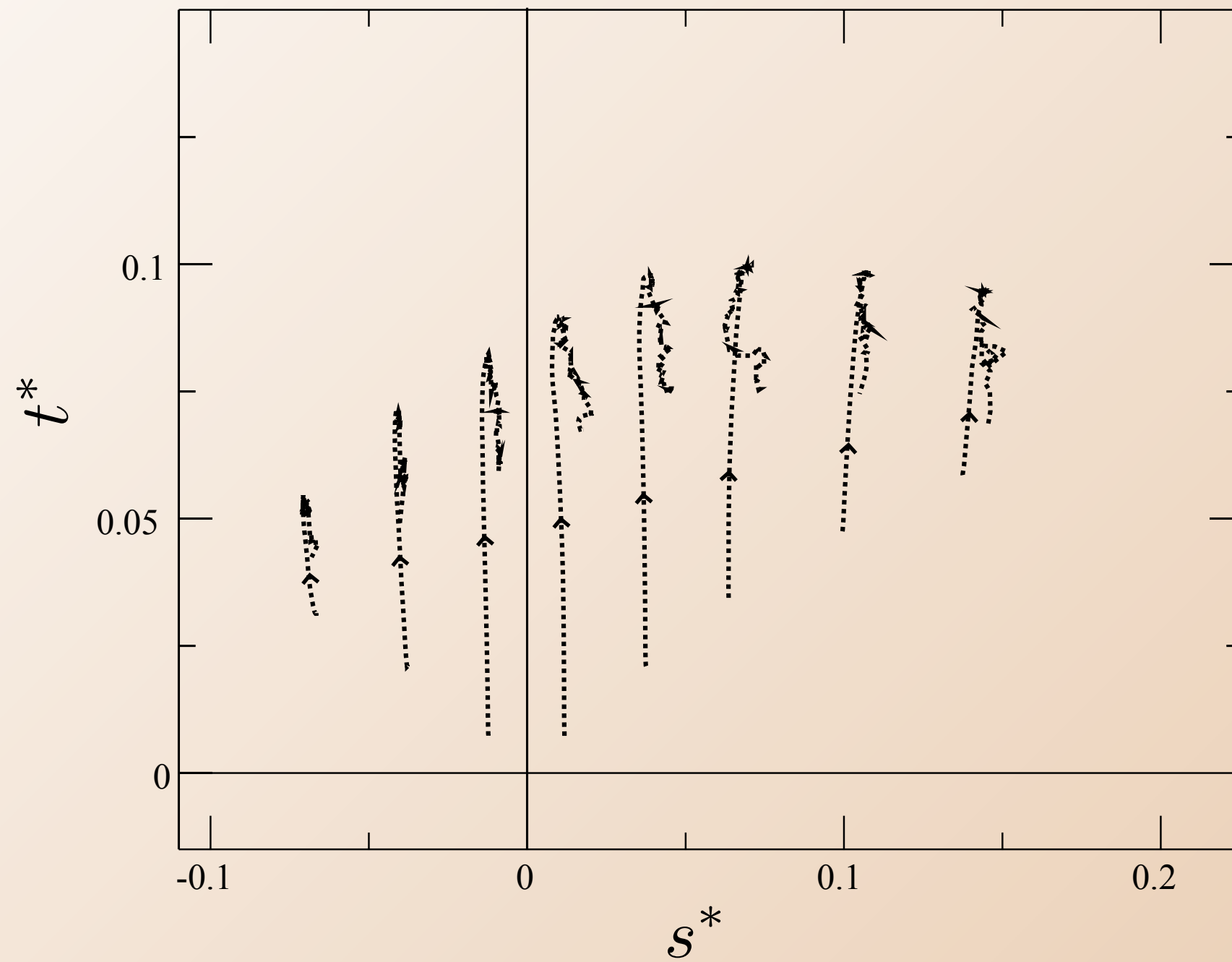
$$s^* \sim \frac{\sigma_1 + \sigma_3}{2}$$

$$t^* \sim \frac{\sigma_1 - \sigma_3}{2}$$

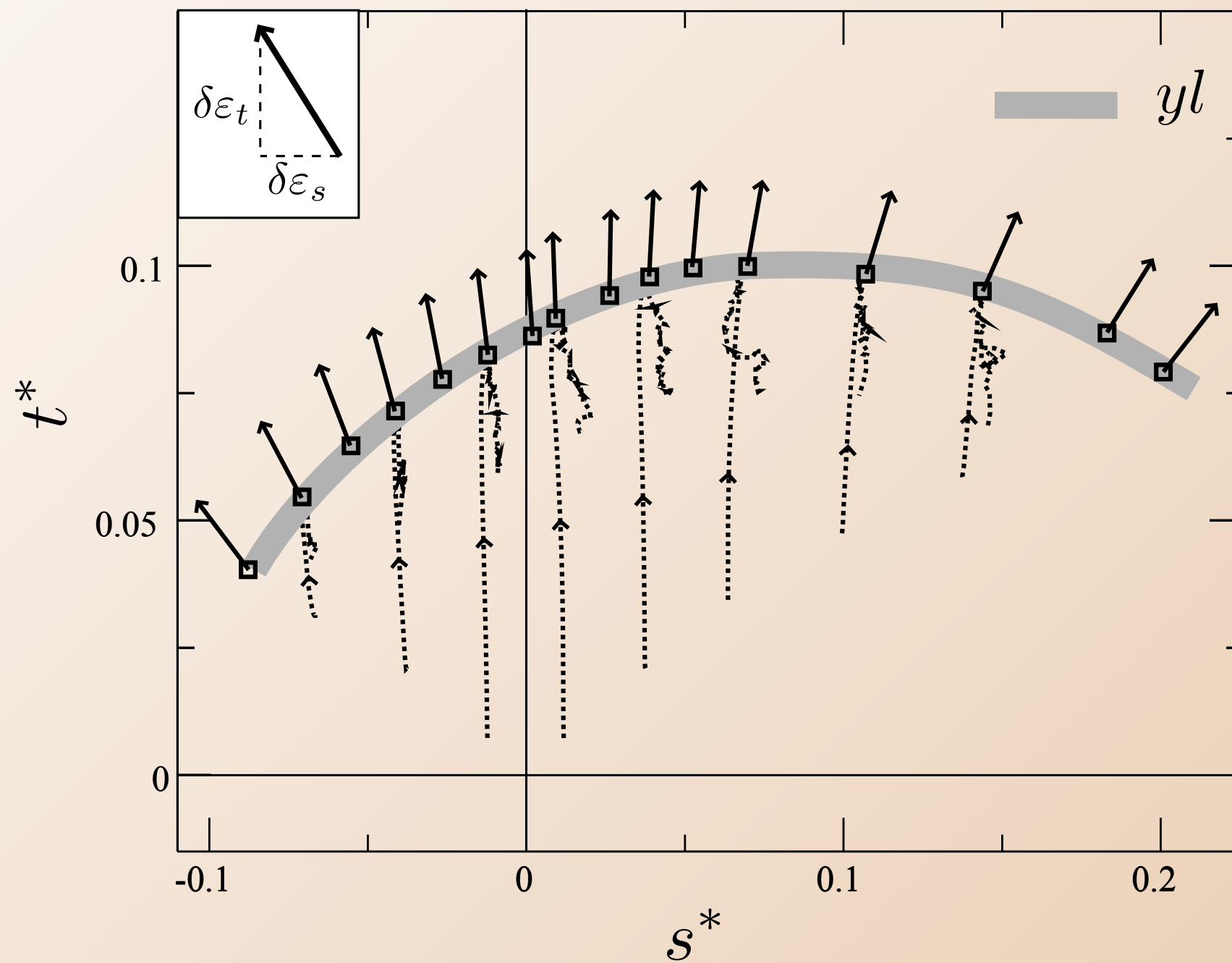
$$\delta\epsilon_s = \delta\epsilon_1 + \delta\epsilon_3$$

$$\delta\epsilon_t = \delta\epsilon_1 - \delta\epsilon_3$$

Yield surface



Yield surface



5. Microscopic analysis

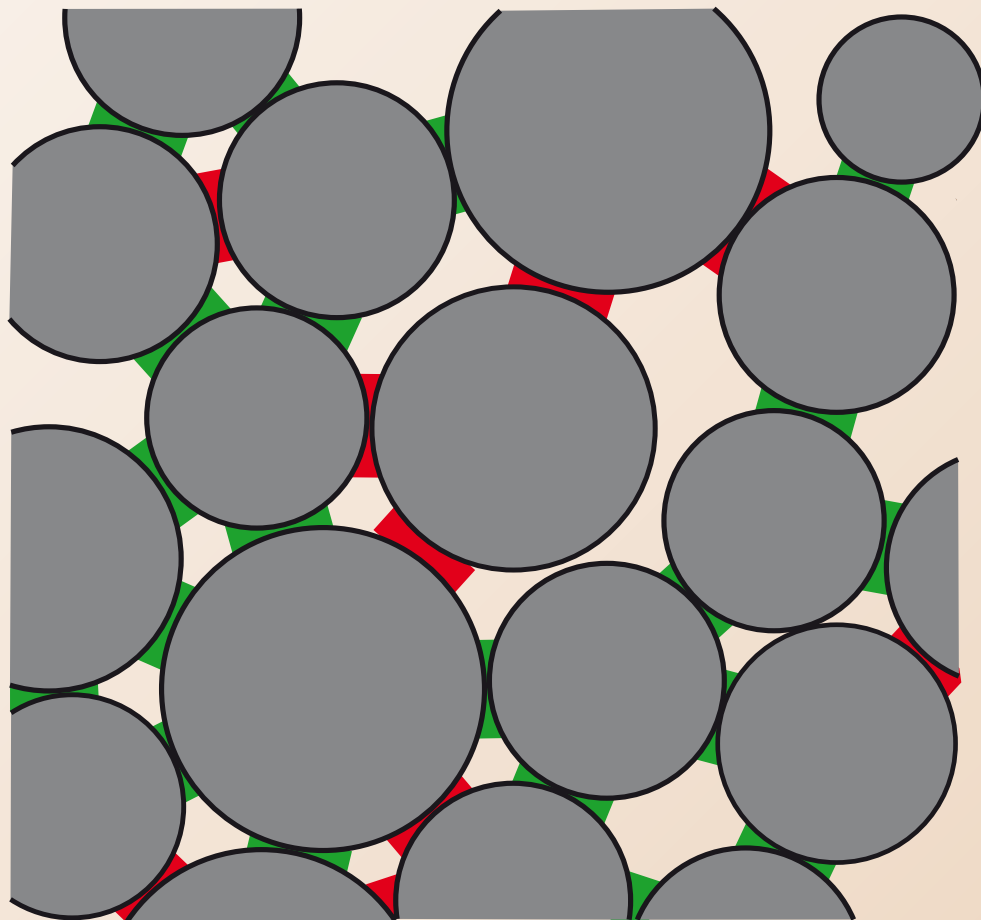
Equilibrium conditions at the contacts scale

$$\begin{aligned} \longrightarrow & \quad f_n = -f_a \\ \longrightarrow & \quad f_t = f_t^{max} \\ \longrightarrow & \quad M = M^{max} \end{aligned}$$

5. Microscopic analysis

Equilibrium conditions at the contacts scale

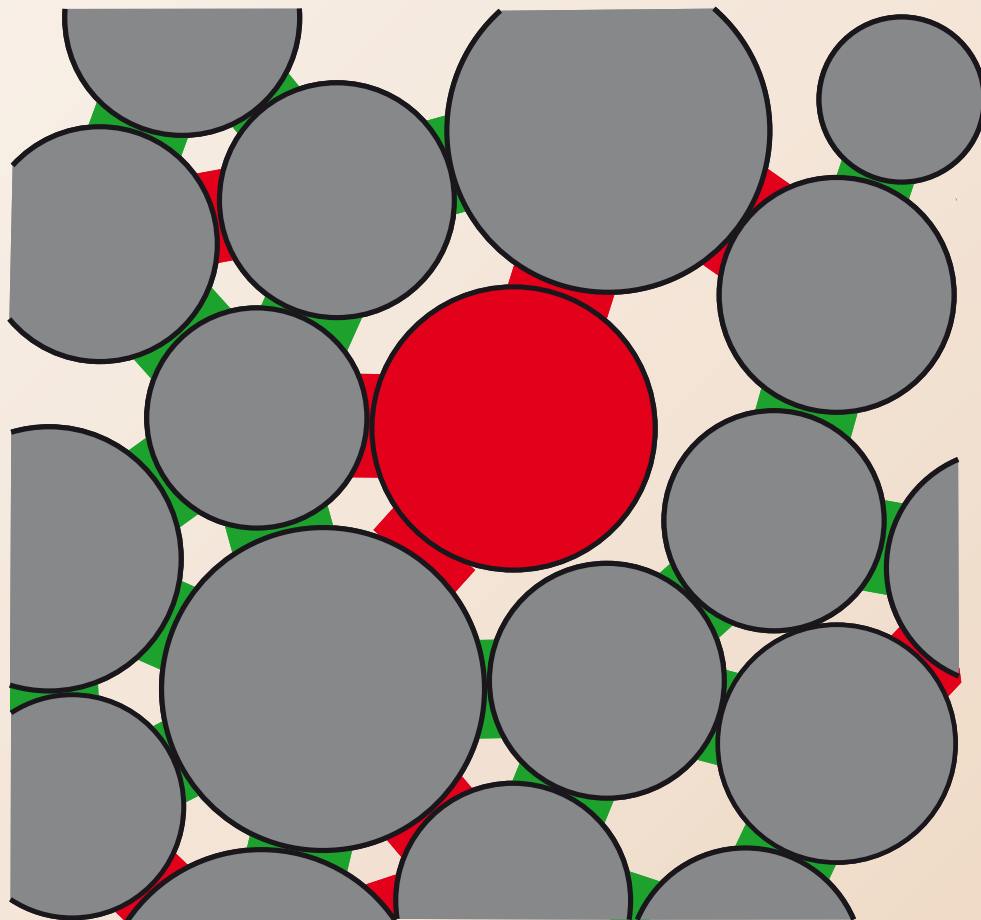
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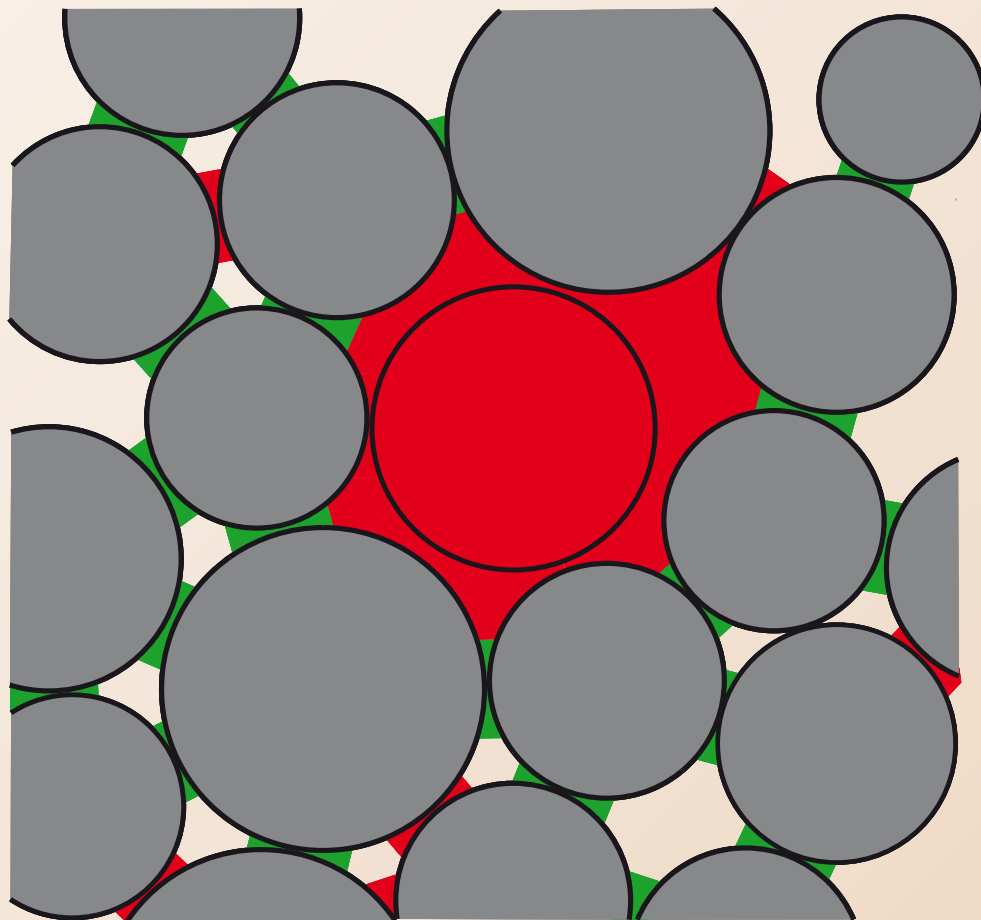


Mobile particles:
particles whose contacts
verify **all** this condition

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Mobile particles:

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Mobile zones:

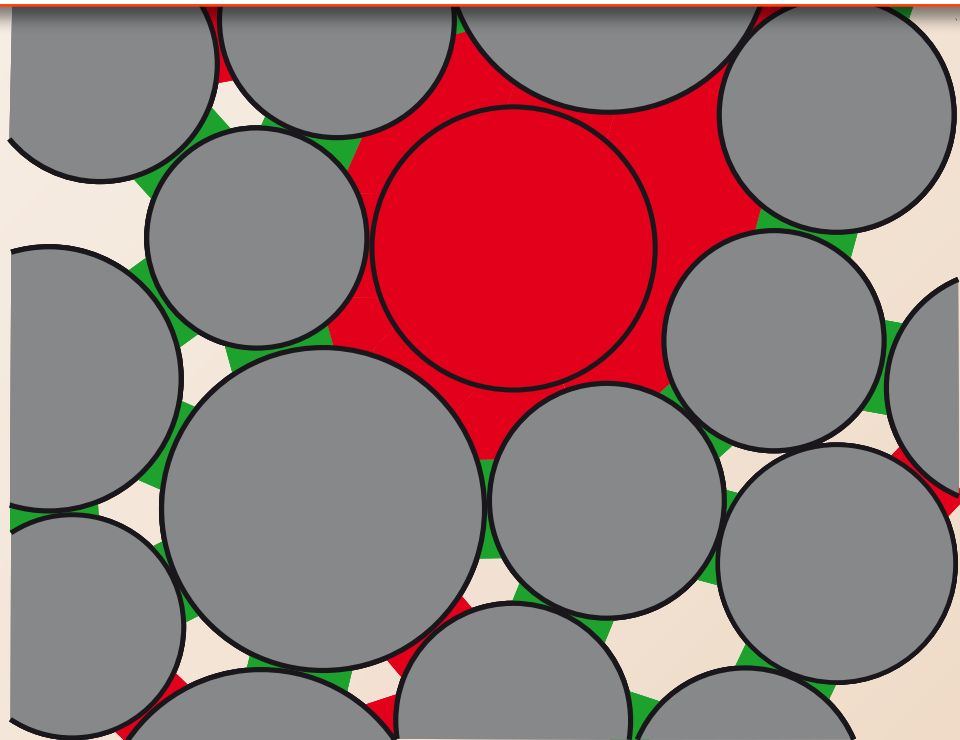
mobile particles **+**
voids that surround them

5. Microscopic analysis

Equilibrium conditions at the contacts scale

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¡Mobile zones are important because they represent regions where yielding is imminent!

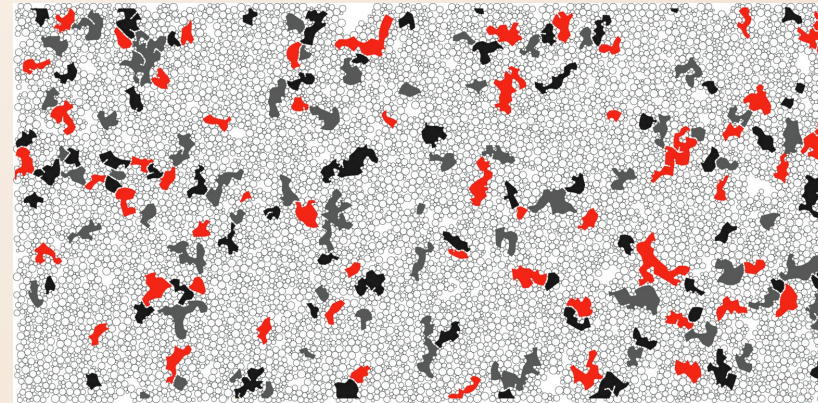


particles whose contacts verify **all** this condition

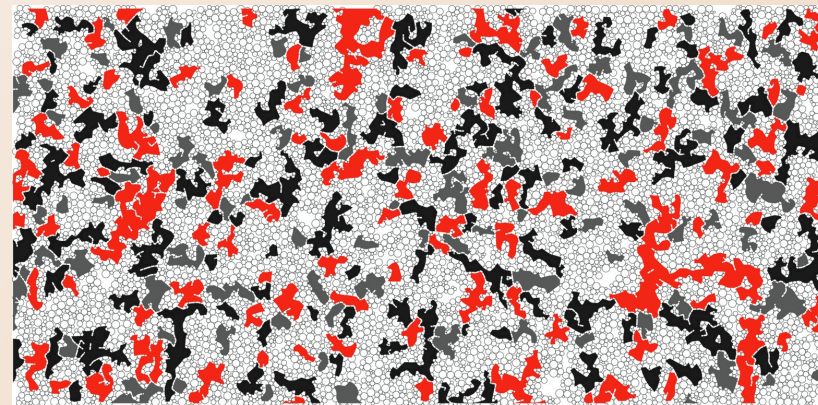
Mobile zones:
mobile particles +
voids that surround them

When increasing the load τ_{wall} from 0 to the yield condition τ_{max} :

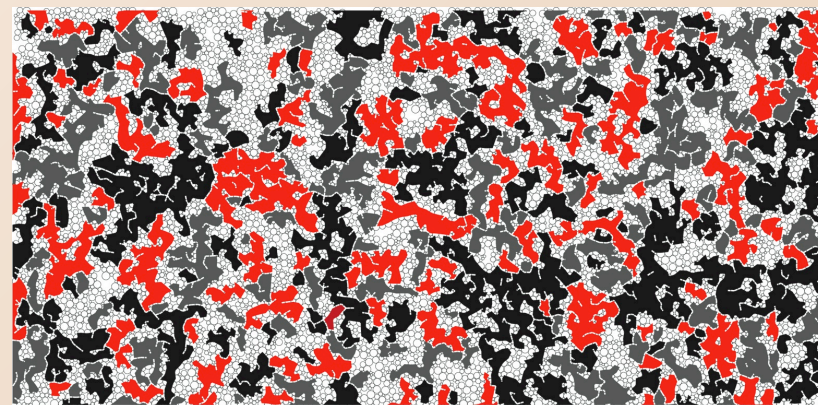
$$\tau_{wall} = 0.25\tau_{max}$$



$$\tau_{wall} = 0.5\tau_{max}$$

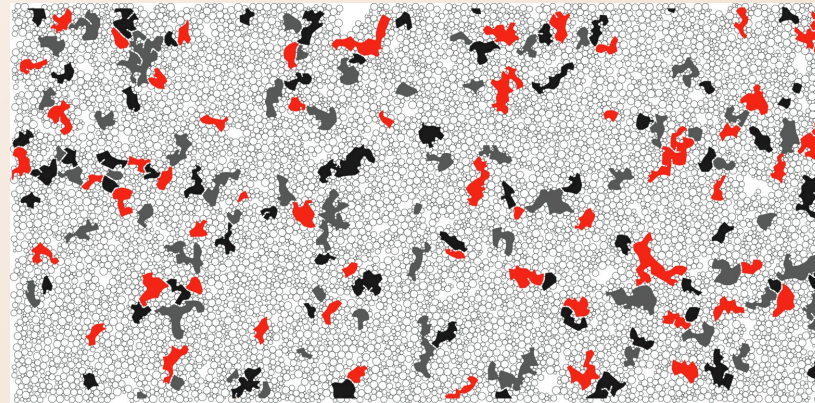


$$\tau_{wall} = 0.75\tau_{max}$$

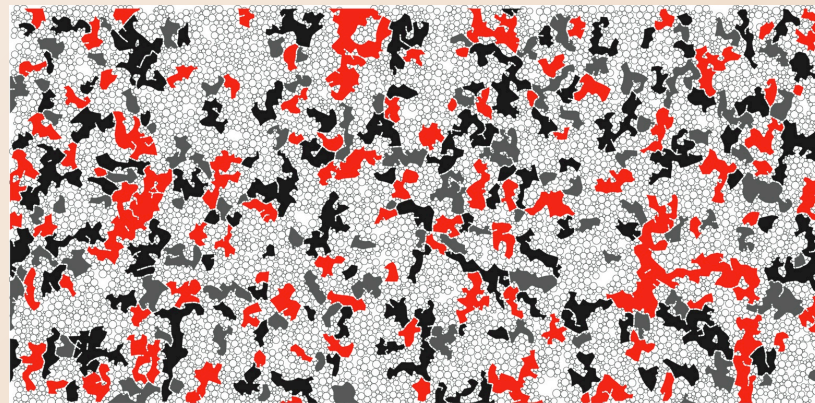


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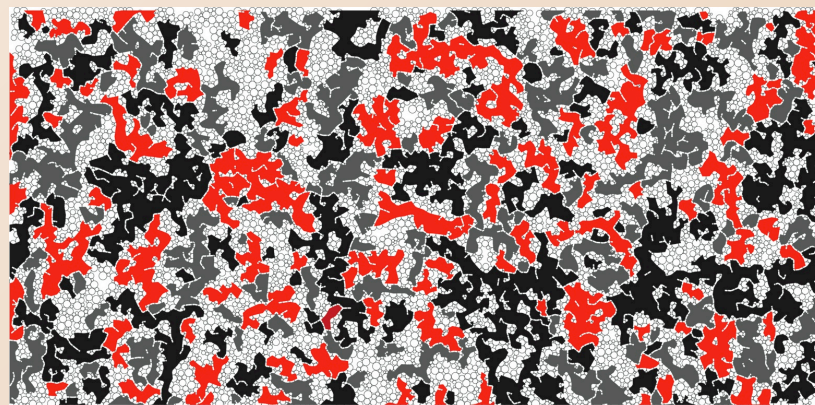
$$\tau_{wall} = 0.25\tau_{max}$$



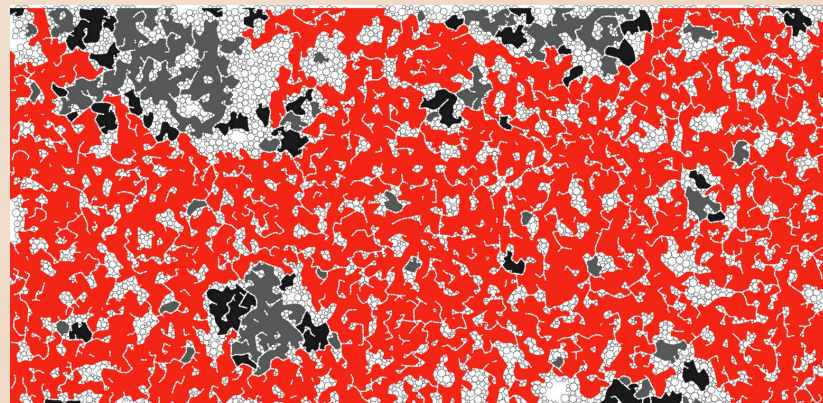
$$\tau_{wall} = 0.5\tau_{max}$$

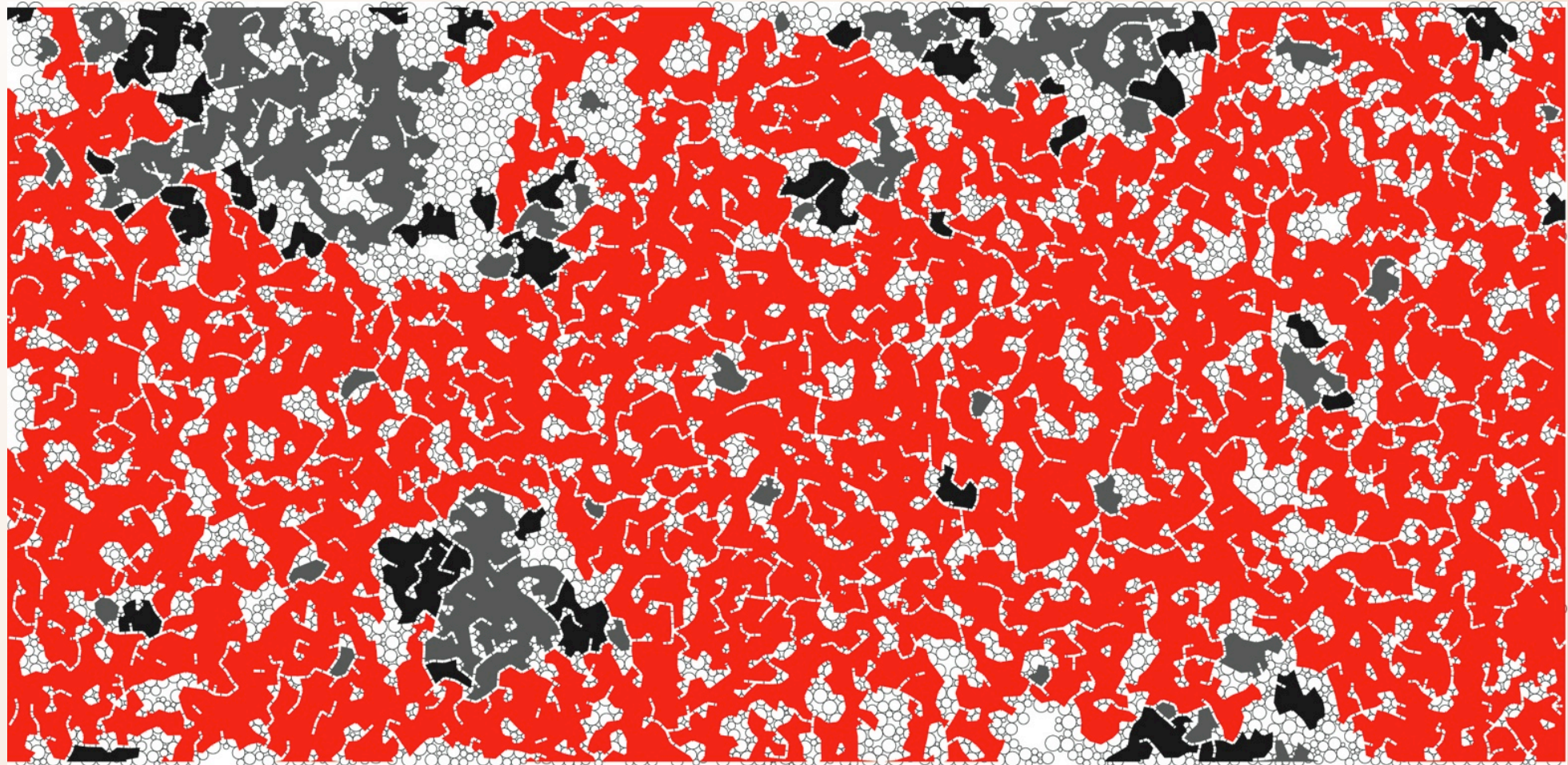


$$\tau_{wall} = 0.75\tau_{max}$$



$$\tau_{wall} = \tau_{max}$$





Yielding can be explained as the percolation of the condition
here called “mobility”

→ phase transition

→ kinematically admissible mechanism
of deformation



Acknowledgements

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Advisors:

Arcesio Lizcano
Alfredo Taboada



Thank you for your attention



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